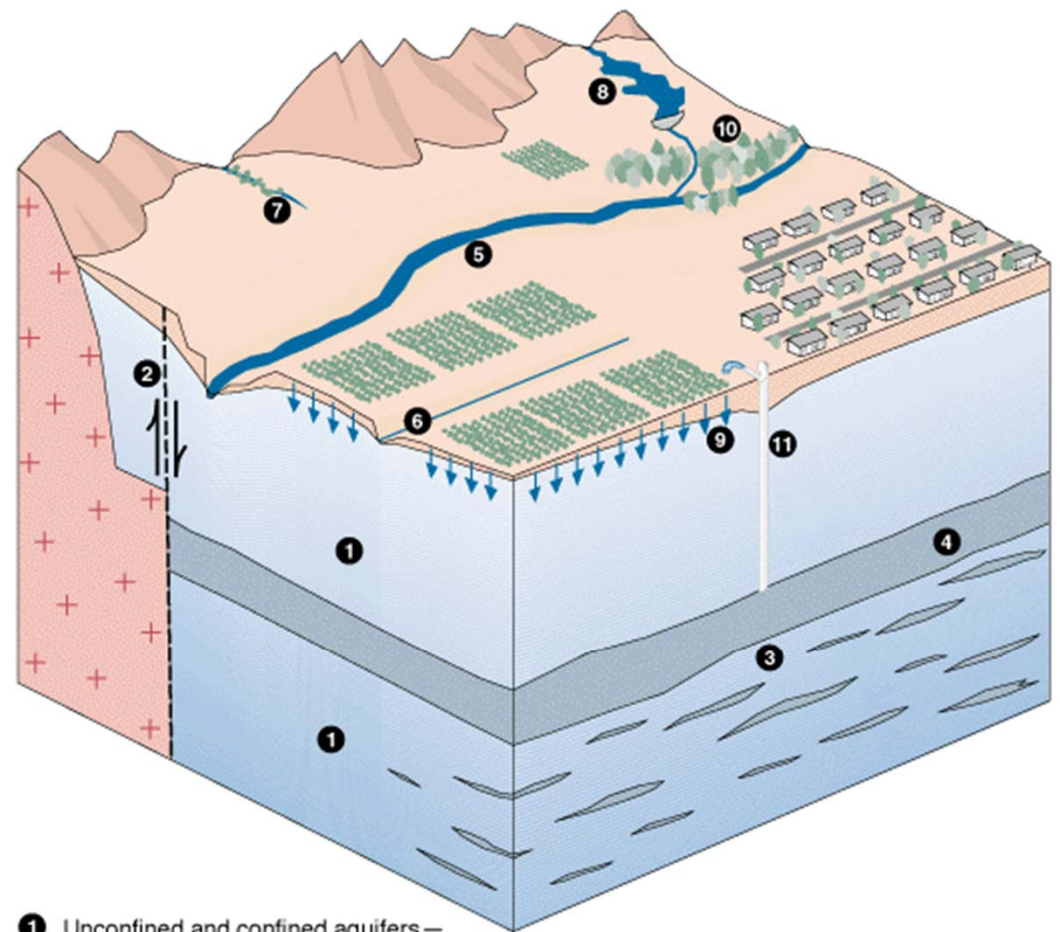


CE EN 547 – BRIGHAM YOUNG UNIVERSITY

# **MODFLOW – Introduction**

## **Organization & Main Packages**

- Developed by McDonald & Harbaugh of the USGS, 1983
- Public Domain
- Most widely used groundwater model
- Steady state or transient saturated flow
- Latest version is MODFLOW 2005
- GMS uses MODFLOW 2000 version

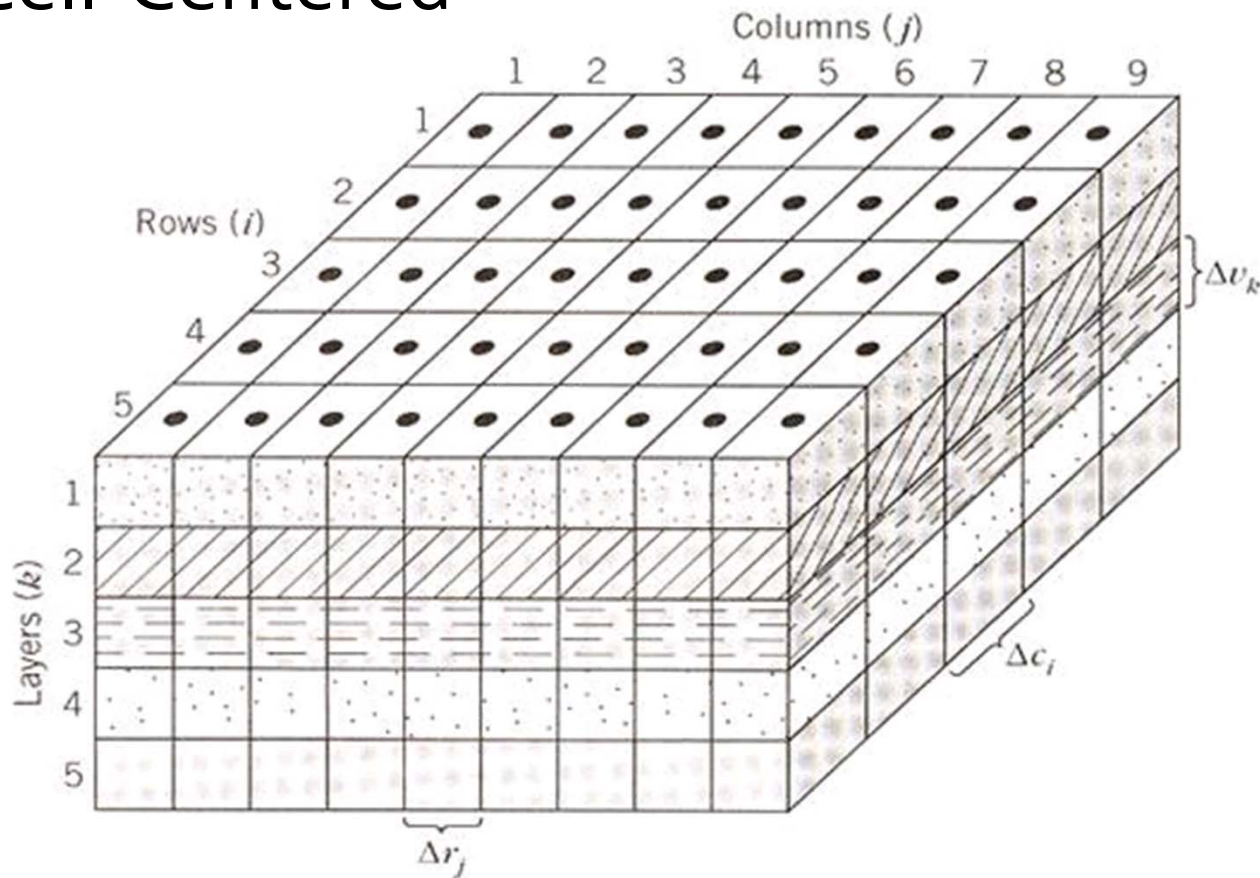


- |  |   |
|--|---|
| ① Unconfined and confined aquifers—<br>Ground-water flow and storage changes | ⑦ Ephemeral streams— Exchange of water<br>with aquifers |
| ② Faults and other barriers— Resistance to<br>horizontal ground-water flow   | ⑧ Reservoirs— Exchange of water with<br>aquifers        |
| ③ Fine-grained confining units and interbeds                                 | ⑨ Recharge from precipitation and irrigation            |
| ④ Confining units— Ground-water flow and<br>storage changes                  | ⑩ Evapotranspiration                                    |
| ⑤ Rivers— Exchange of water with aquifers                                    | ⑪ Wells— Withdrawal or recharge at speci-<br>fied rates |
| ⑥ Drains and springs— Discharge of water<br>from aquifers                    |   |

Figure 1. Features of an aquifer system that can be simulated by MODFLOW.

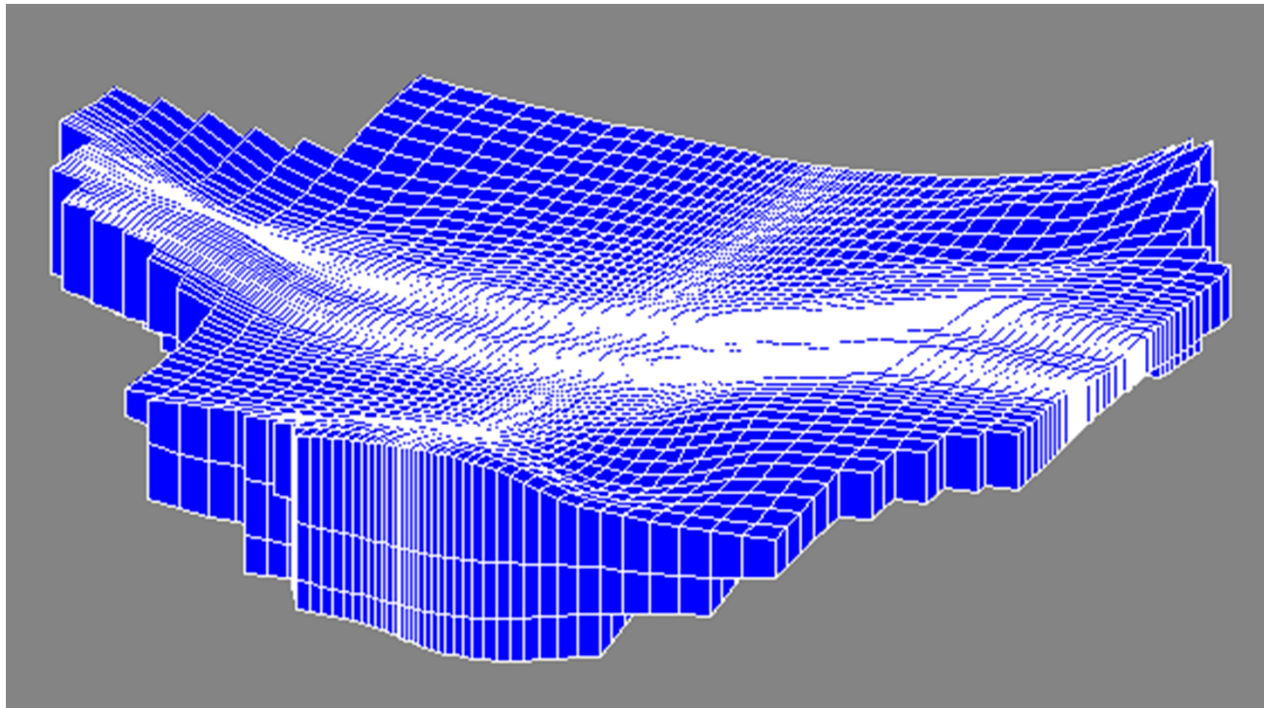
# Finite Difference Model

- 3D Cartesian Grid
- Cell-Centered



# Grid Geometry

- Orthogonal in  $xy$
- Thickness varies in  $z$



# Governing Equation

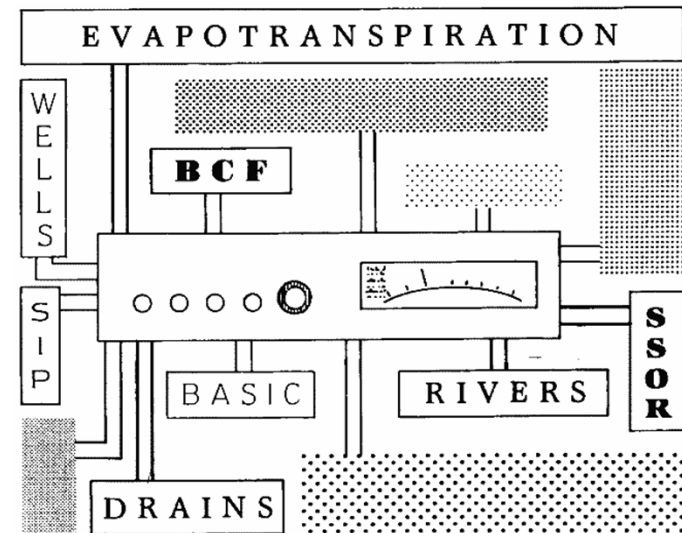
$$\frac{\partial}{\partial x} \left( K_{xx} \frac{\partial h}{\partial x} \right) + \frac{\partial}{\partial y} \left( K_{yy} \frac{\partial h}{\partial y} \right) + \frac{\partial}{\partial z} \left( K_{zz} \frac{\partial h}{\partial z} \right) - W = S_s \frac{\partial h}{\partial t}$$

where:

$K_{xx}, K_{yy}, K_{zz}$  = values of hyd. cond. along xyz axes  
 $h$  = total head  
 $W$  = Sources and sinks  
 $S_s$  = Specific storage  
 $t$  = time

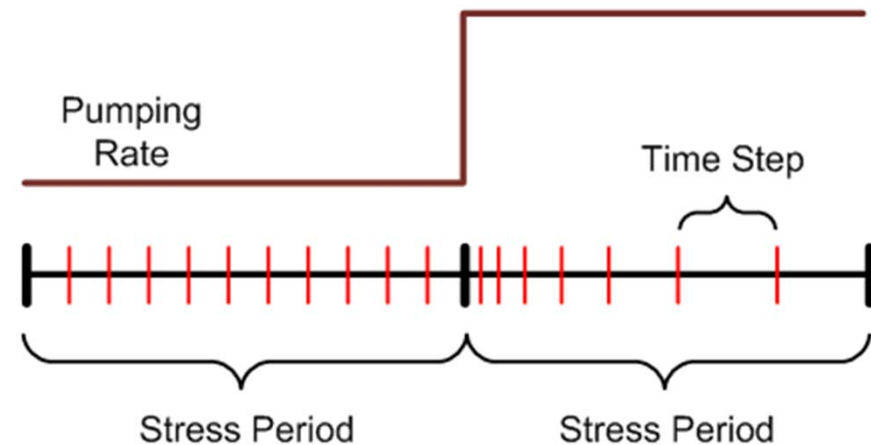
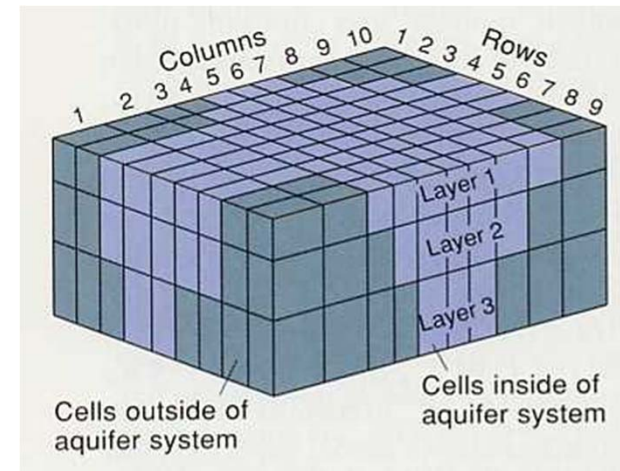
# Processes & Packages

- MODFLOW is divided into a series of processes & packages.
- Major tasks are organized as processes
- More specific tasks are performed by packages
- Each process may use one or more packages



# Global Process

- Spatial discretization
  - # rows, cols, layers
  - Top/bottom elevations
- Temporal discretization
  - Stress periods
  - Time steps
- Units
- Package Selection



# Ground Water Flow Process

- Formulation and solution of the ground water flow equation by the FD method
- Main part of MODFLOW code
- Includes
  - Flow package (BCF, LPF, or HUF)
  - Source/sink packages
  - Solvers

# Other Processes

- Observation Process
  - Observed heads and flows
  - Used for calibration
- SEN Process
  - Sensitivity analysis
  - Calibration
- PES Process
  - Automated parameter estimation (calibration)

# Packages

- Required Packages
  - Basic
  - Global
  - Output Control
  - Flow Package (BCF, LPF, HUF)
  - Solver (SIP, SSOR, PCG, GMG, etc.)
- List-Based Stress Packages
  - River
  - Stream-Aquifer Interaction
  - Drain
- General Head
- Well
- Lake
- Changing Head Boundary
- Array-Based Stress Packages
  - Recharge
  - Evapotranspiration
- Other
  - Horizontal Flow Barrier

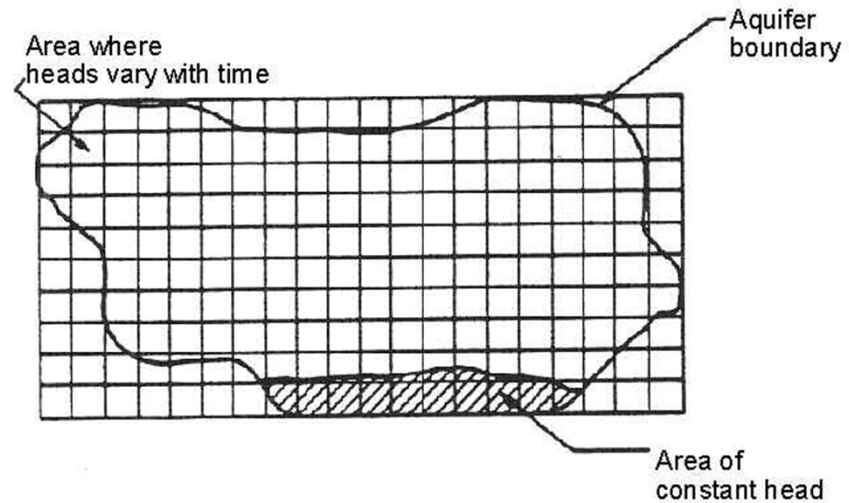
# Basic Package

- Starting Heads Array

- Provides initial set of heads for iterative solver.
- Defines head values at specified head cells

- IBOUND Array

- Array of integers
- Three possible values
  - zero = inactive
  - negative = specified head
  - positive = variable head



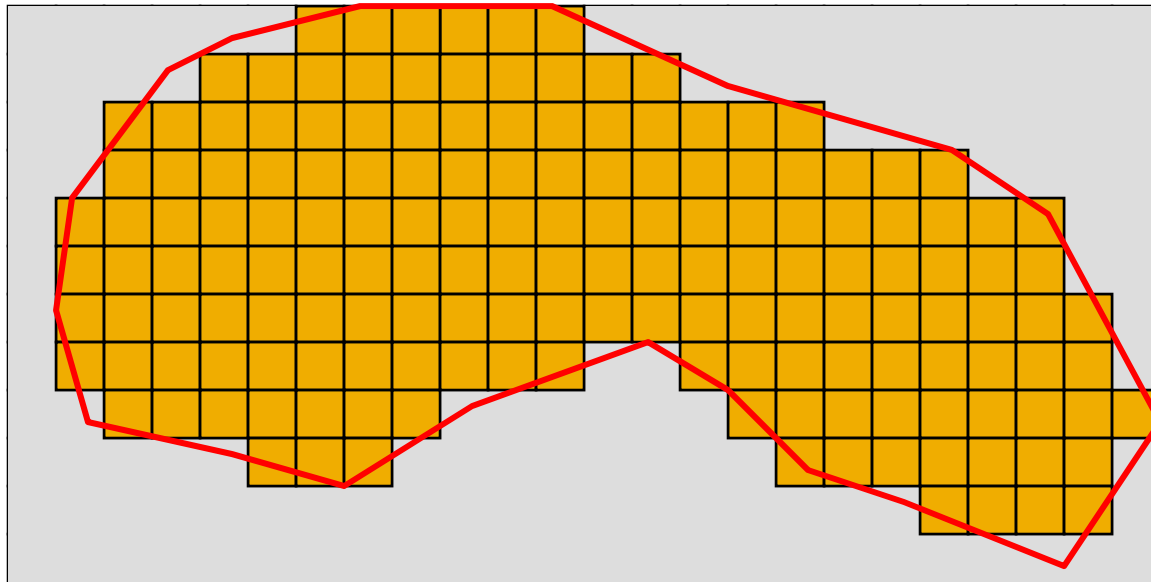
0	1	1	1	1	1	0	0	0	0	0	0	0	1	1	1	1	1	0	0
1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0
1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0
0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0
0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0
0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1
0	0	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	0
0	0	0	0	0	0	1	1	1	1	1	1	1	1	1	1	1	1	0	0
0	0	0	0	0	0	0	-1	-1	-1	-1	-1	-1	-1	-1	-1	-1	0	0	0

IBOUND Codes  
 < 0 Constant head  
 = 0 No flow  
 > 0 Variable head

Figure 19-1 (figure 19, McDonald and Harbaugh, 1988).  
 Example of the boundary array (IBOUND) for a single layer.

# Active/Inactive Zones

Cells outside problem domain are marked as inactive



# Virginia Coastal Plain Model

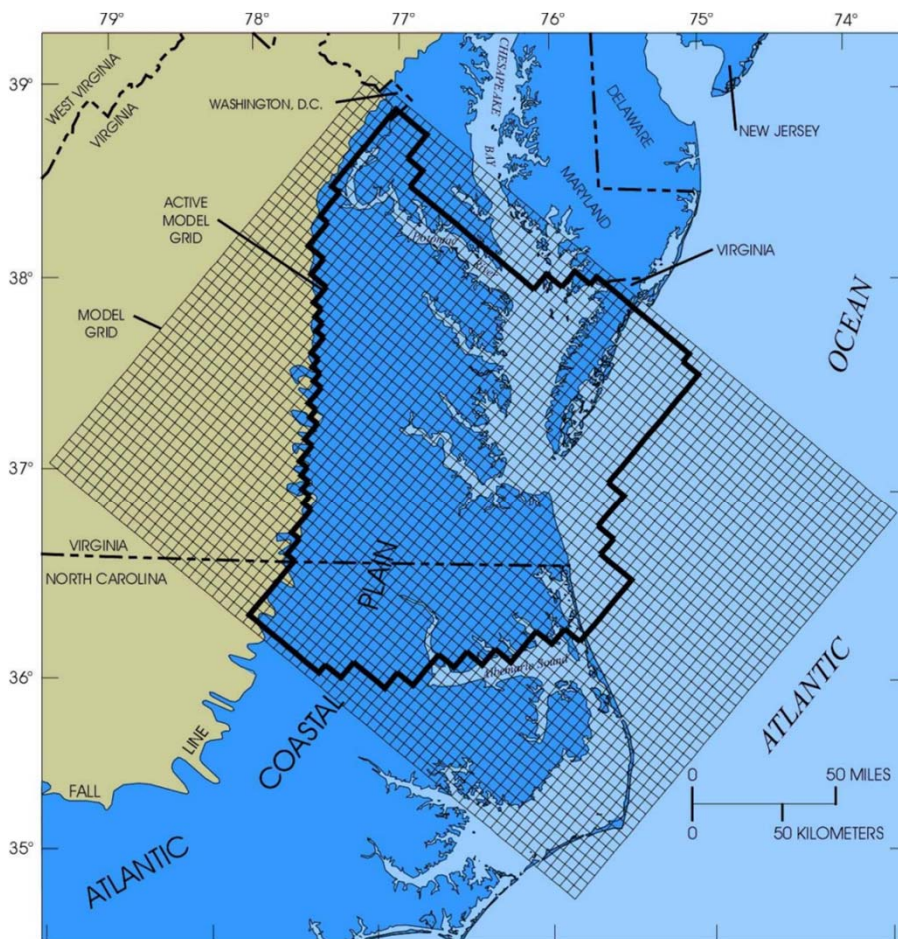


Figure 3. Ground-water-flow model grid in the Virginia Coastal Plain.

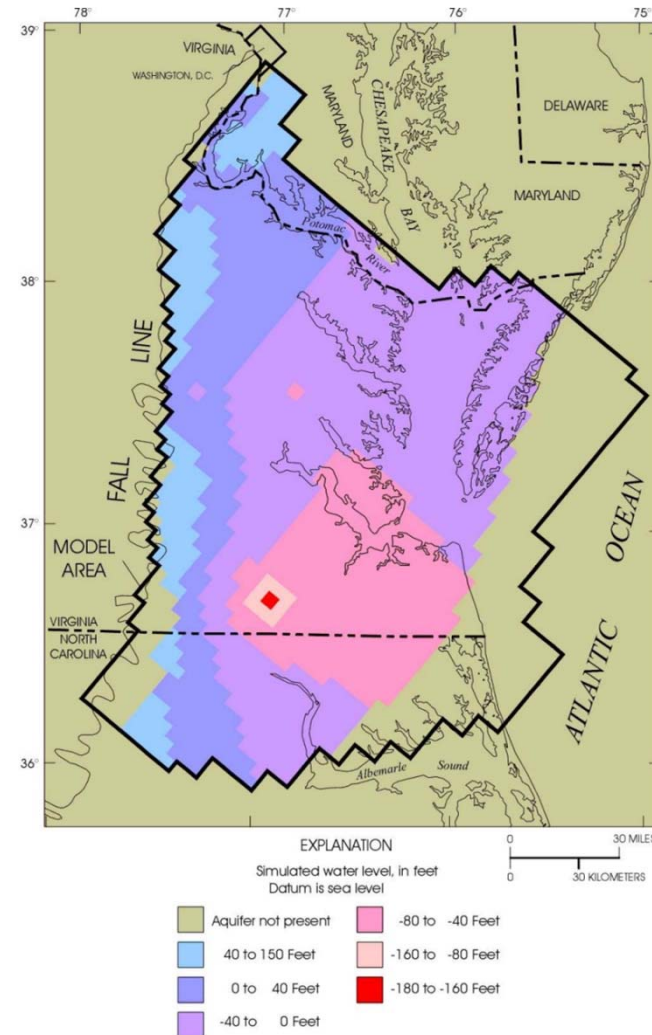


Figure 31. Simulated water levels for 1978-80 in the middle Potomac aquifer.

# Flow Packages

- Three options
  - Block-Centered Flow (BCF)
  - Layer Property Flow (LPF)
  - Hydrogeologic Unit Flow (HUF)
- One of the three packages must be used

# BCF Package

- Original flow package
- Each layer is assigned a layer type
- Layer data are entered (depending on type)
  - Horizontal K
  - Bottom elevation
  - Transmissivity
  - Leakance
  - etc.

# Layer Property Flow (LPF) Package

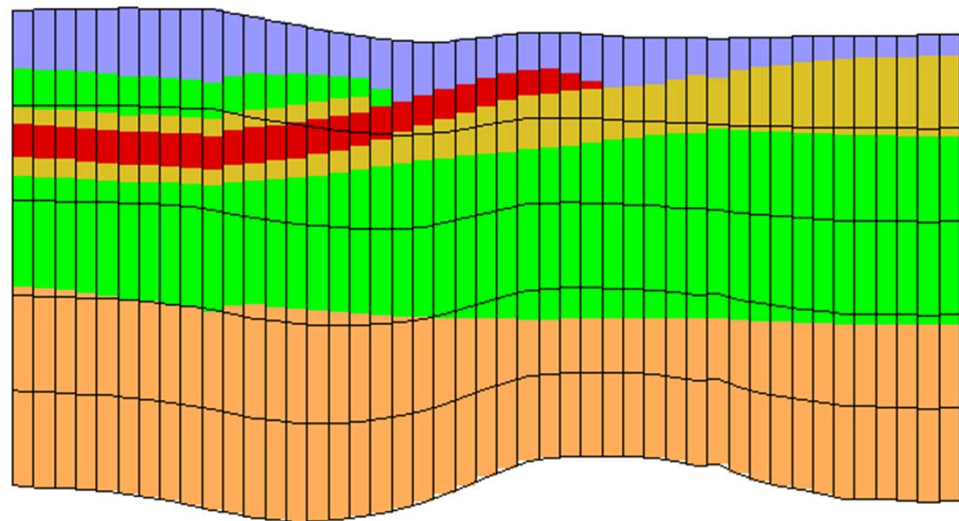
- User enters  $K_h$ ,  $K_v$  and storage terms for all layers, regardless of type
- $K_v$  can be entered as directly or in terms of vertical anisotropy
- Horizontal anisotropy entered on a cell-by-cell basis
- Two layer types
  - Confined
  - Convertible

# LPF Property Input

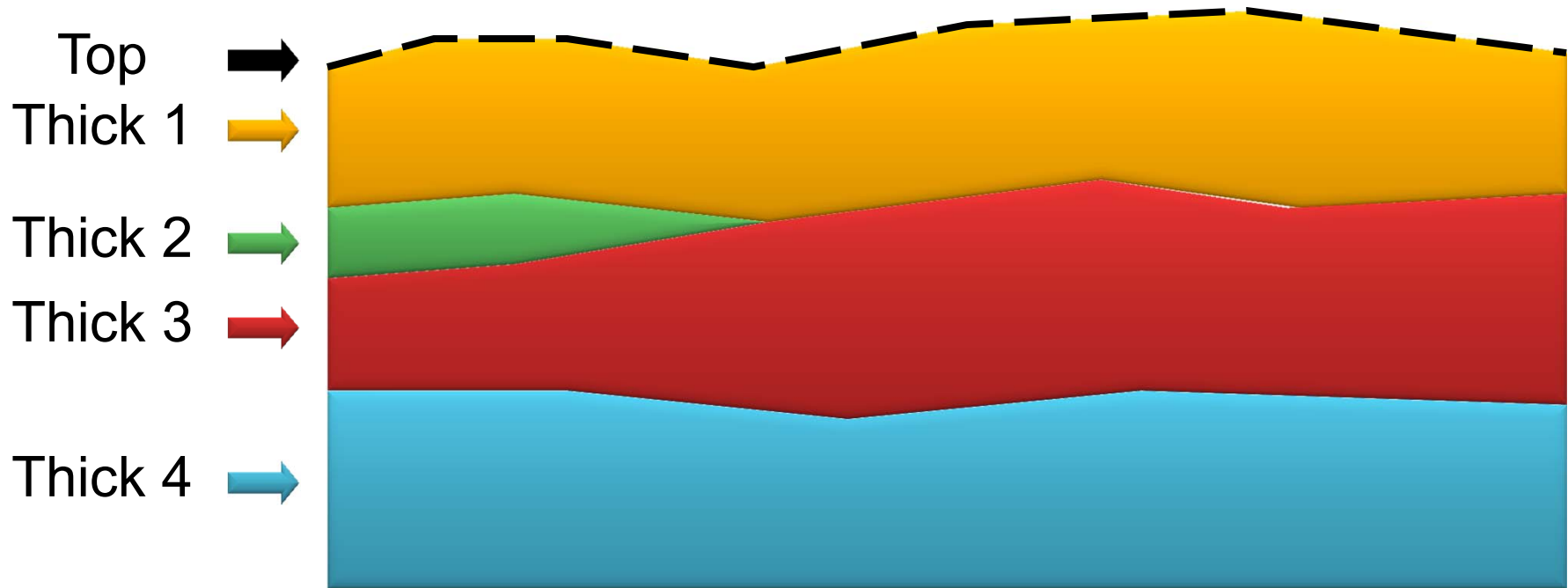
- Two options for inputting hydraulic properties:
  - Array input
    - one value per cell
  - Material id approach
    - Each cell is assigned a material id
    - Properties are inherited from material

# Hydrogeologic Unit Flow (HUF) Package

- Aquifer stratigraphy represented in a grid-independent fashion
- Equivalent  $K_h$ ,  $K_v$  computed at runtime

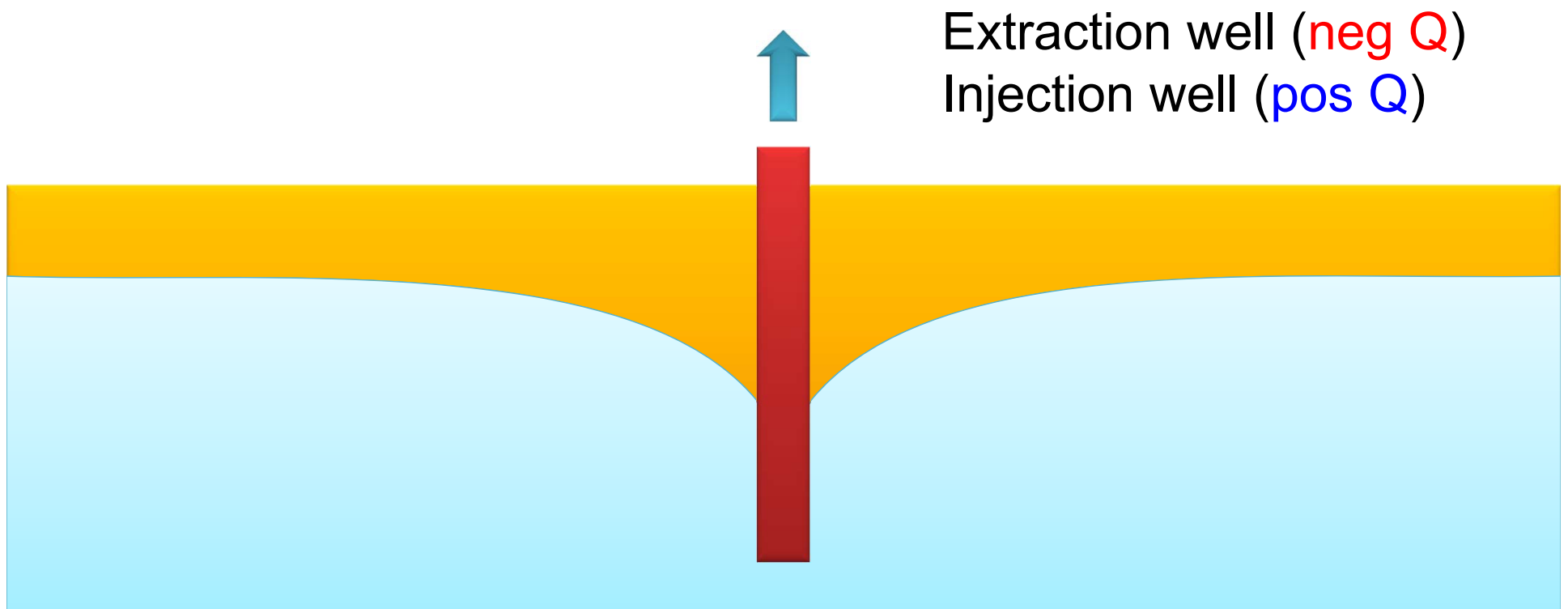


# HUF Arrays



# Well Package

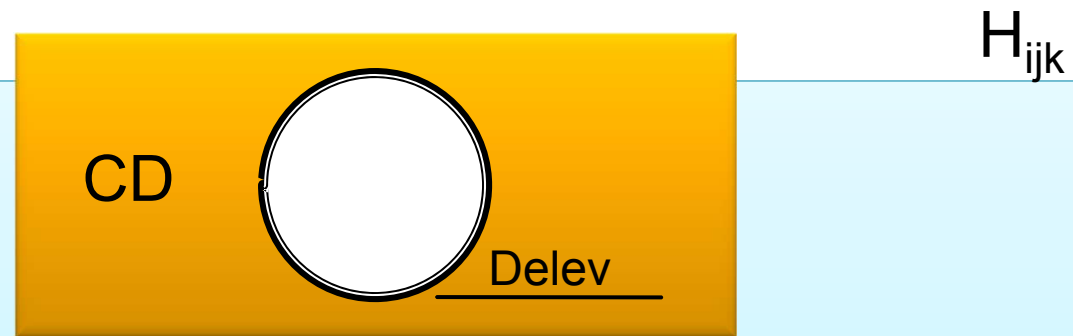
- Assigned to individual cells
- $Q$  can be steady state or transient



# Drain Package

- Assigned to individual cells
- Used to simulate
  - Agricultural drains
  - Springs
  - Creek beds
- Required parameters
  - Elevation
  - Conductance

# Drains

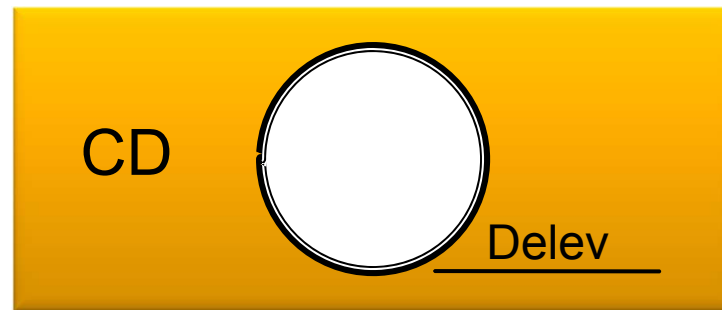


When the head is above the drain elevation:

$$Q = CD (H_{ijk} - Delev) \text{ or}$$

$$Q = CD (Delev - H_{ijk}) \text{ for proper sign on } Q$$

# Drains



$H_{ijk}$

When the head is below the drain elevation:

$$Q = 0$$

# Conductance

Darcy's Law:

$$q = k \frac{\Delta h}{L} A$$

where

$q$  = flow rate

$k$  = hydraulic conductivity

$\Delta h$  = head difference

$L$  = flow length

$A$  = gross cross-sectional area

# Conductance, Cont.

Darcy's law can be rewritten as:

$$q = C \cdot \Delta h$$

where

$$C = \frac{kA}{L}$$

The appropriate values for  $k$ ,  $A$ , and  $L$  must be determined on a case-by-case basis

# Recharge Package

- One value assigned to each vertical column
- Represents recharge due to precipitation
- Can be steady state or transient
- Infiltration rate must be assigned in correct units [L/T]



# Factors Affecting Recharge Rate

- Rainfall
- Runoff
  - Slope
  - Soil type
  - Land use
- Evapotranspiration
  - Soil type
  - Vegetation